## Globally Challenged:

Are U.S. Students Ready to Compete?

## The latest on each state's international standing in math and reading

Paul E. Peterson•Ludger Woessmann•Eric A. Hanushek • Carlos X. Lastra-Anadón


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The views expressed here are our own and should not be attributed to any other party or to the institutions with which we are affiliated.


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## Table of Contents

Executive Summary ..... v
Introduction ..... 3
Comparing U.S. Students with Peers in Other Countries ..... 4
Proficiency in Math ..... 6
Proficiency in Reading ..... 11
Performance of U.S. Ethnic and Racial Groups ..... 11
White students ..... 12
Students from college-educated families ..... 15
Are the Proficiency Standards the Same for Math as for Reading? ..... 17
What Do These Findings Mean? ..... 17
Appendix:
Differences in Math Performance of the High School Classes of 2009 and 2011 ..... 20
Performing the Crosswalk ..... 21
Identifying the Class of 2011 ..... 22
Critiques of PISA ..... 23
References ..... 33
Biographical Sketches ..... 34
Figures
Figure 1
Percentage of students in the Class of 2011 at the proficient level in mathin U.S. states and foreign jurisdictions participating in PISA 20098
Figure 2
Percentage of students in the Class of 2011 at the proficient level in reading in U.S. states and foreign jurisdictions participating in PISA 2009 ..... 12
Figure 3Percentage of students in the Class of 2011 at the proficient level inmath and reading, by race and ethnicity15
Figure 4
Estimated increase in U.S. annual economic growth from improved mathematics proficiency ..... 19
Figure A. 1
Percentage of white students in the Class of 2011 in U.S. states at theproficient level in math and percentage of all students at that level inforeign jurisdictions participating in PISA 200924
Figure A. 2Percentage of white students in the Class of 2011 in U.S. states at theproficient level in reading and percentage of all students at that levelin foreign jurisdictions participating in PISA 200924

Figure A. 3
Percentage of students in the Class of 2011 with at least one college-educated parent in U.S. states at the proficient level in math and percentage of all students at that level in foreign jurisdictions participating in PISA 2009

Figure A. 4
Percentage of students in the Class of 2011 with at least one college-educated parent in U.S. states at the proficient level in reading and percentage of all students at that level in foreign jurisdictions participating in PISA 2009
Figure A. 5
Percentage of students in the Class of 2011 at the advanced level in math in U.S. states and foreign jurisdictions participa ting in PISA 2009

## Tables

Table 1
Percentages of all students in the Class of 2011 at the proficient level in math per state. Foreign jurisdictions with similar and higher percentages at the proficient level in math in overall student population10

Table 2
Percentages of all students in the Class of 2011 at the proficient level in reading per state. Foreign jurisdictions with similar and higher percentages at the proficient level in reading in overall student population.
Table A. 1
Percentages of white students in the Class of 2011 at the proficient level in math per state. Foreign jurisdictions with similar and higher percentages at the proficient level in math in overall student population . . . . . . . . . . 28

Table A. 2
Percentages of white students in the Class of 2011 at the proficient level in reading per state. Foreign jurisdictions with similar and higher percentages at the proficient level in reading in overall student population29

Table A. 3
Percentages of students in the Class of 2011 with at least one college-educated parent at the proficient level in math per state. Foreign jurisdictions with similar and higher percentages at the proficient level in math in overall student population30

Table A. 4
Percentages of students in the Class of 2011 with at least one college-educated parent at the proficient level in reading per state. Foreign jurisdictions with similar and higher percentages at the proficient level in reading in overall student population31

## Table A. 5

Percentages of all students in the class of 2011 at the advanced level in math per state. Foreign jurisdictions with similar and higher percentages at the advanced level in math in overall student population 32


America faces many challenges...but the enemy I fear most is complacency. We are about to be hit by the full force of global competition. If we continue to ignore the obvious task at hand while others beat us at our own game, our children and grandchildren will pay the price. We must now establish a sense of urgency."

## Executive Summary

$\mathbf{A}_{\mathrm{t}}$ a time of persistent unemployment, especially among the less skilled, many wonder whether our schools are adequately preparing students for the 21 st-century global economy. This is the second study of student achievement in global perspective prepared under the auspices of Harvard's Program on Education Policy and Governance (PEPG). In the 2010 PEPG report, "U.S. Math Performance in Global Perspective," the focus was on the percentage of U.S. public and private school students performing at the advanced level in mathematics. ${ }^{1}$ The current study continues this work by reporting the percentage of public and private school students identified as at or above the proficient level (a considerably lower standard of performance than the advanced level) in mathematics and reading for the most recent cohort for which data are available, the high-school graduating Class of 2011.

## Proficiency in Mathematics

U.S. students in the Class of 2011, with a 32 percent proficiency rate in mathematics, came in 32nd among the nations that participated in PISA. Although performance levels among the countries ranked 23rd to 31 st are not significantly different from that of the United States, 22 countries do significantly outperform the United States in the share of students reaching the proficient level in math. In six countries plus Shanghai and Hong Kong, a majority of students performed at the proficient level, while in the United States less than one-third did. For example, 58 percent of Korean students and 56 percent of Finnish students were proficient. Other countries in which a majority—or near majority-of students performed at or above the proficient level included Switzerland, Japan, Canada, and the Netherlands. Many other nations also had math proficiency rates well above that of the United States, including Germany (45 percent), Australia (44 percent), and France (39 percent).

Shanghai topped the list with a 75 percent math proficiency rate, well over twice the 32 percent rate of the United States. However, Shanghai students are from a prosperous metropolitan area within China, with over three times the GDP per capita of the rest of that country, so their performance is more appropriately compared to Massachusetts and Minnesota, which are similarly favored and are the top performers among the U.S. states. When this comparison is made, Shanghai still performs at a distinctly higher level. Only a little more than half ( 51 percent) of Massachusetts students are proficient

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1. Hanushek, Peterson, and Woessmann (2010).
in math, while Minnesota, the runner-up state, has a math proficiency rate of just 43 percent.

Only four additional states-Vermont, North Dakota, New Jersey, and Kansas-have a math proficiency rate above 40 percent. Some of the country's largest and richest states score below the average for the United States as a whole, including New York (30 percent), Missouri (30 percent), Michigan (29 percent), Florida ( 27 percent), and California ( 24 percent).

## Proficiency in Reading

The U.S. proficiency rate in reading, at 31 percent, compares reasonably well to those of most European countries other than Finland. It takes 17th place among the nations of the world, and only the top 10 countries on PISA outperform the United States by a statistically significant amount. In Korea, 47 percent of the students are proficient in reading. Other countries that outrank the United States include Finland (46 percent), Singapore and New Zealand (42 percent), Japan and Canada (41 percent), Australia (38 percent), and Belgium (37 percent).

Within the United States, Massachusetts is again the leader, with 43 percent of 8th-grade students performing at the NAEP proficient level in reading. Shanghai students perform at a higher level, however, with 55 percent of young people proficient in reading. Within the United States, Vermont is a close second to its neighbor to the south, with a 42 percent proficiency rate. New Jersey and South Dakota come next, with 39 and 37 percent of the students identified as proficient in reading. Students living in California (about oneeighth of the U. S. school-age population) are statistically tied with their peers in Slovakia and Spain.

## Data and Approach

Increasingly, states, and the federal government itself, have established performance levels that students are asked to reach. A national proficiency standard was set by the board that governs the National Assessment of Educational Progress (NAEP), which is administered by the U.S. Department of Education and generally known as the nation's report card.

We provide information on student performance in both reading and mathematics, but our main concern is the relative performance of U.S. students in mathematics. That information is obtained by comparing student performance on NAEP math and reading tests with the performance of students from across the world on similar examinations. If the NAEP exams are the
nation's report card, the world's report card is assembled by the Organization for Economic Co-operation and Development (OECD), which administers the Program for International Student Assessment (PISA) to representative samples of 15-year-old students in 65 of the world's school systems.

Since the United States participates in the PISA examinations, it is possible to make direct comparisons between the average performance of U.S. students nationwide and that of their peers elsewhere. But because PISA exams do not set proficiency standards in the same way that NAEP exams do, one cannot calculate the percent proficient in the various countries of the world without performing a crosswalk between NAEP and PISA. Once that crosswalk has been performed, it is possible not only to provide estimates of the percentage of students who are proficient in various countries but also to view from an international perspective the performance of students from particular social groups as well as those living in each state.

A crosswalk is made possible by the fact that representative (but separate) samples of the high-school graduating Class of 2011 took both the NAEP and PISA math and reading examinations. NAEP tests were taken in 2007 when the Class of 2011 was in 8th grade and PISA tested 15-year-olds in 2009, most of whom are members of the Class of 2011. Given that NAEP identified 32 percent of U.S. 8th-grade students as proficient in math, the PISA equivalent is estimated by calculating the minimum score reached by the top-performing 32 percent of U.S. students participating in the 2009 PISA test.

## Performance of U.S. Ethnic and Racial Groups

The percentage proficient in the United States varies considerably across students from different racial and ethnic backgrounds. While 42 percent of white students were identified as proficient in math, only 11 percent of African American students, 15 percent of Hispanic students, and 16 percent of Native Americans were so identified. Fifty percent of students with an ethnic background from Asia and the Pacific Islands, however, were proficient in math.

In reading, 40 percent of white students and 41 percent of those from Asia and the Pacific Islands were identified as proficient. Only 13 percent of African American students, 5 percent of Hispanic students, and 18 percent of Native American students were so identified.

Given the disparate performance among students from various cultural backgrounds, it may be worth inquiring as to whether differences between the United States and other countries are attributable to the substantial minority population within the United States. To examine that question, we compare

U.S. students in the

Class of 2011, with
a 32 percent proficiency rate in mathematics, came in 32nd among the nations that participated in PISA.


While the 42 percent math proficiency rate for U.S. white students is much higher than the averages for students from
African America and Hispanic backgrounds, U.S. white students are still surpassed by all students in 16 other countries.
2. Quoted in the STEM Education Coalition's website http://www.stemedcoalition.org/, Accessed June 13, 2011.
U.S. white students to all students in other countries. We do this not because we think this is the right comparison, but simply to consider the oft-expressed claim that comparisons do not take into account the fact that the United States is a much more diverse society than many of the high-performing countries.

While the 42 percent math proficiency rate for U.S. white students is much higher than the averages for students from African American and Hispanic backgrounds, U.S. white students are still surpassed by all students in 16 other countries. A better than 25-percentage-point gap exists between the performance of U.S. white students and the percentage of all students deemed proficient in Korea and Finland. White students in the United States trail well behind all students in countries such as Japan, Germany, Belgium, and Canada.

In reading, the picture looks better. As we mentioned above, only 40 percent of white students are proficient, but that proficiency rate would place the United States at 9th in the world.

## What Do These Findings Mean?

The United States could enjoy a remarkable increment in its annual GDP growth per capita by enhancing the math proficiency of U.S. students. Increasing the percentage of proficient students to the levels attained in Canada and Korea would increase the annual U.S. growth rate by 0.9 percentage points and 1.3 percentage points, respectively. Since long-term average annual growth rates hover between 2 and 3 percentage points, that increment would lift growth rates by between 30 and 50 percent.

When translated into dollar terms, these magnitudes become staggering. If one calculates these percentage increases as national income projections over an 80-year period (providing for a 20-year delay before any school reform is completed and the newly proficient students begin their working careers), a back-of-the-envelope calculation suggests gains of nothing less than $\$ 75$ trillion over the period. That averages out to around a trillion dollars a year. Even if you tweak these numbers a bit in one direction or another to account for various uncertainties, you reach the same bottom line: Those who say that student math performance does not matter are clearly wrong.

Charles Vest, former president of the Massachusetts Institute of Technology, has warned, "America faces many challenges...but the enemy I fear most is complacency. We are about to be hit by the full force of global competition. If we continue to ignore the obvious task at hand while others beat us at our own game, our children and grandchildren will pay the price. We must now establish a sense of urgency." ${ }^{2}$

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Sixty-five countries participated in the math and reading examinations administered by the Program for
International Student Assessment (PISA).


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By Paul E. Peterson, Ludger Woessmann, Eric A. Hanushek, and Carlos X. Lastra-Anadón

At a time of persistent unemployment, especially among the less skilled, many wonder whether our schools are adequately preparing students for the 21st-century global economy. Despite high unemployment rates, firms are experiencing shortages of educated workers, outsourcing professional-level work to workers abroad, and competing for the limited number of employment visas set aside for highly skilled immigrants. As President Barack Obama said in his 2011 State of the Union address, "We know what it takes to compete for the jobs and industries of our time. We need to out-innovate, out-educate, and out-build the rest of the world." ${ }^{1}$

The challenge is particularly great in math, science, and engineering. According to Internet entrepreneur Vinton Cerf, "America simply is not producing enough of our own innovators, and the cause is twofold-a deteriorating K-12 education system and a national culture that does not emphasize the importance of education and the value of engineering and science." ${ }^{2}$ To address the issue, the Science, Technology, Engineering, and Math (STEM) Education Coalition was formed in 2006 to "raise awareness in Congress, the Administration, and other organizations about the critical role that STEM education plays in enabling the U.S. to remain the economic and technological leader of the global marketplace." ${ }^{3}$

Tales of shortages of educated talent appear regularly in the media. According to a CBS News report, 22 percent of American businesses say they are ready to

"We know what it takes to compete for the jobs and industries of our time.
We need to out-innovate, out-educate, and out-build the rest of the world."

- President Barack Obama

1. Office of the Press Secretary,

White House Office, "Remarks by the President in the State of the Union Address," January 25, 2011 (http://www.whitehouse.gov/ the-press-office/2011/01/25/ remarks-president-state-union-address) 2. Vinton G. Cerf: "How to fire up US Innovation," Wall Street Journal, April 12 2011, (http://online.wsj.com/article/ SB10001424052748704461304576216911954 533514.html)
3. STEM Education Coalition website, STEM Ed Coalition Objectives, accessed June 13, 2011 at http://www.stemedcoalition.org/ about-us/
4. Cynthia Bowers, CBS News Report: "Skilled Labor Shortage Frustrates Employees," August 12, 2010 (http:// www.cbsnews.com/stories/2010/08/11/ eveningnews/main6764731.shtml)
5. Bartsch (2009).
6. McKinsey Global Institute (2011).
7. Hanushek, Peterson, and Woessmann (2010).
8. NAEP has three levels: basic, proficient, and advanced. We report here the rates of those who are at or above the proficient level. 9. See Appendix for an international comparison of the math performance of the Class of 2011 at the advanced level.
hire if they can find people with the right skills. As one factory owner put it, "It's hard to fill these jobs because they require people who are good at math, good with their hands, and willing to work on a factory floor." ${ }^{4}$ According to a Bureau of Labor Statistics report, of the 30 occupations projected to grow the most rapidly over the next decade, nearly half are professional jobs that require at least a college degree. ${ }^{5}$ On the basis of these projections, McKinsey's Global Institute estimates that over the next few years there will be a gap of nearly 2 million workers with the necessary analytical and technical skills. ${ }^{6}$ In this report, we examine the capacity of American schools to meet these needs.

## Comparing U.S. Students with Peers in Other Countries

This is the second study of student achievement in global perspective prepared under the auspices of Harvard's Program on Education Policy and Governance (PEPG). In the 2010 PEPG report, "U.S. Math Performance in Global Perspective," the focus was on the percentage of U.S. public and private school students performing at the advanced level in mathematics. ${ }^{7}$ Specifically, the study compared the math performance of students in the high-school graduating Class of 2009 with that of their peers around the world. The current study continues this work by reporting the percentage of public and private school students identified as at or above the proficient level (a considerably lower standard of performance than the advanced level) in mathematics and reading for the most recent cohort for which data are available, the high-school graduating Class of 2011. ${ }^{8}$ Just as it is critical that the United States produce a segment of students who perform at the very highest level, so is it essential that a much larger portion of the next generation be proficient enough in math and reading to perform effectively in an economy that requires ever-increasing technical skill. ${ }^{9}$

At one time it was left to teachers and administrators to decide exactly what level of math proficiency should be expected of students. But, increasingly, states, and the federal government itself, have established performance levels that students are asked to reach. A national proficiency standard was set by the board that governs the National Assessment of Educational Progress (NAEP), which is administered by the U.S. Department of Education and generally known as the nation's report card.

In 2007, just 32 percent of 8 th graders in public and private schools in the United States performed at or above the NAEP proficiency standard in mathematics, and 31 percent performed at or above that level in reading. When more than two-thirds of students fail to reach a proficiency bar, it raises serious questions: Are U.S. schools failing to teach their students adequately?

## Percentages and Scores for Proficient Students

In the United States, in 2007, the share of 8 th-grade students identified as proficient on the NAEP math examination was 32.192 percent. The minimum math score on the PISA examination obtained in 2009 by the highest-performing 32.192 percent of all U.S. students was estimated to be 530.7. To cover a broad content area while ensuring that testing time does not become excessive, the tests employ matrix sampling. No student takes the entire test, and scores are aggregated across students. For individual student observations, results are thus estimates of performance obtained by averaging five plausible values, as PISA and NAEP administrators recommend.

Comparable numbers for the other categories are as follows:
Reading proficiency: 31.223 percent of U.S. students are proficient on the NAEP, which corresponds to a score of 550.4 on PISA.

Advanced math: 6.998 percent of U.S. students scored at the advanced level on the NAEP, which corresponds to 623.2 on PISA.

Advanced reading: 2.767 percent of U.S. students scored at the advanced level on the NAEP, which corresponds to 678.1 on PISA.

Or has NAEP set its proficiency bar at a level beyond the normal reach of a student in 8th grade?

One way of tackling such questions is to take an international perspective. Are other countries able to lift a higher percentage-or even a majority-of their students to or above the NAEP proficiency bar? Another approach is to look at differences among states. What percentage of students in each state is performing at a proficient level? How does each state compare to students in other countries? Those are the questions we shall explore in this report.

We provide information on student performance in both reading and mathematics, but our main concern is the relative performance of U.S. students in mathematics. This emphasis is based on prior research that has identified numeracy or math skills as primary determinants of advances in a nation's economic productivity. ${ }^{10}$ It is also, as we shall see, the subject area in which the United States performs well below many other countries in the industrialized world.

That information is obtained by comparing student performance on NAEP math and reading tests with the performance of students from across the world on similar examinations. If the NAEP exams are the nation's report card, the world's report card is assembled by the Organization for Economic Co-operation and Development (OECD), which administers the Program

"America simply is not producing enough of our own innovators, and the cause is twofolda deteriorating K-12 education system and a national culture that does not emphasize the importance of education and the value of engineering and science."

- Vinton Cerf, Internet entrepreneur

10. For a discussion of this literature, see Hanushek and Woessmann (2008). In addition, it seems probable that math performances are more precisely calibrated across different languages and cultures than reading performances are.
11. In the 2007 edition of the other largescale international study that compares performance of students across countries, the Trends in Mathematics and Science Study (TIMSS 2007), the United States as well as the individual states of Massachusetts and Minnesota participated. This enables the comparison of those two particular states with other countries' performance for TIMSS. See note 19, below. For a further comparison of TIMSS and PISA, see Hanushek, Peterson, and Woessmann (2010), Appendix.

TIMSS 2007 surveyed fewer countries in the industrialized world than PISA does, concentrating instead on gathering similar information from among developing countries. The total number of countries surveyed by TIMSS 2007 was 48 , while PISA surveyed 65 jurisdictions in 2009. TIMSS content has a less applied emphasis than PISA does. Nonetheless, at the country level, scores on PISA and TIMSS are highly correlated (Hanushek and Woessmann, 2008).
12. "Development of the Assessment," NAEP: available online at http://nces.ed.gov/ nationsreportcard/mathematics/howdevelop. asp, accessed June 13, 2011.
for International Student Assessment (PISA) to representative samples of 15-year-old students in 65 of the world's school systems (which, to simplify the presentation, we shall refer to as countries; Hong Kong, Macao, and Shanghai are not independent nations but are nonetheless included in PISA reports). Since its launch in 2000, the PISA test has emerged as the yardstick by which countries measure changes in their performance over time and the level of their performance relative to that of other countries.

Since the United States participates in the PISA examinations, it is possible to make direct comparisons between the average performance of U.S. students nationwide and that of their peers elsewhere. But because PISA exams do not set proficiency standards in the same way that NAEP exams do, one cannot calculate the percent proficient in the various countries of the world without performing a crosswalk between NAEP and PISA. Once that crosswalk has been performed, it is possible not only to provide estimates of the percentage of students who are proficient in various countries but also to view from an international perspective the performance of students from particular social groups as well as those living in each state. ${ }^{11}$

A crosswalk is made possible by the fact that representative (but separate) samples of the high-school graduating Class of 2011 took both the NAEP and PISA math and reading examinations. NAEP tests were taken in 2007 when the Class of 2011 was in 8th grade and PISA tested 15-year-olds in 2009, most of whom are members of the Class of 2011. Given that NAEP identified 32 percent of U.S. 8th-grade students as proficient in math, the PISA equivalent is estimated by calculating the minimum score reached by the top-performing 32 percent of U.S. students participating in the 2009 PISA test. (See methodological sidebar on page 5 for details of these scores and Appendix for further discussion of the crosswalk.)

## Proficiency in Math

According to the National Center for Education Statistics (NCES), which administers NAEP, the determination of proficiency in any given subject at a particular grade level "was the result of a comprehensive national process [which took into account]...what hundreds of educators, curriculum experts, policymakers, and members of the general public thought the assessment should test. After the completion of the framework, the NAEP [subject] Committee worked with measurement specialists to create the assessment questions and scoring criteria." ${ }^{12}$ In other words, NAEP's concept of proficiency is not based on any objective criterion, but instead reflects a consensus on what should be known by students who have reached a certain educational stage. NAEP

## NAEP Definition of Math Proficiency at the 8th Grade Level and PISA's Definition of Proficiency Level Three

Eighth-graders performing at the proficient level should be able to conjecture, defend their ideas, and give supporting examples. They should understand the connections between fractions, percents, decimals, and other mathematical topics such as algebra and functions.... Quantity and spatial relationships in problem solving and reasoning should be familiar to them, and they should be able to convey underlying reasoning skills beyond the level of arithmetic.... These students should make inferences from data and graphs, apply properties of informal geometry, and accurately use the tools of technology. Students at this level should...be able to calculate, evaluate, and communicate results within the domain of statistics and probability. ${ }^{i}$

Roughly comparable is PISA's Level 3 standard, defined as follows:
At Level 3 students can execute clearly described procedures, including those that require sequential decisions. They can select and apply simple problem solving strategies. Students at this level can interpret and use representations based on different information sources and reason directly from them. They can develop short communications reporting their interpretations, results and reasoning. ${ }^{\text {ii }}$

## Sample NAEP Question at 8th Grade Proficiency Level

Three tennis balls are to be stacked one on top of another in a cylindrical can. The radius of each tennis ball is 3 centimeters. To the nearest whole centimeter, what should be the minimum height of the can? Explain why you chose the height that you did. Your explanation should include a diagram.
If you chose 18 cm from the list of five choices, you are in the company of the 28 percent of U.S. 8th graders from the Class of 2011 who answered correctly. ${ }^{\text {iii }}$

## Sample PISA Question at Proficiency Level Three

Mark (from Sydney, Australia) and Hans (from Berlin, Germany) often communicate with each other using 'chat' on the Internet. They have to log on to the Internet at the same time to be able to chat. To find a suitable time to chat, Mark looked up a chart of world times and found the following:


At 7:00 pm in Sydney, what time is it in Berlin? The answer is 10 am. ${ }^{\text {iv }}$


The U.S. proficiency rate in reading, at 31 percent, compares reasonably well to those of most European countries other than Finland.
i. NAEP's definitions of the different levels of math achievement http://nces.ed.gov/ nationsreportcard/mathematics/achieveall.asp. Accessed on June 13, 2011.
ii. OECD (2009a).
iii. Question come from NAEP's online past questions database, http://nces.ed.gov/ nationsreportcard/itmrlsx/ search.aspx?subject=mathematics.
Accessed on June 13, 2011.
iv. Shiel, Perkins, Close, and Oldham (2007).

## Percentage of students in the class of 2011 at the proficient level in math in U.S. states and foreign


13. NAEP's definitions of the different levels of achievement http://nces.ed.gov/ nationsreportcard/mathematics/achieveall. asp. Accessed on June 13, 2011.
14. OECD (2009a).
says that 8th graders, if proficient, "understand the connections between fractions, percents, decimals, and other mathematical topics such as algebra and functions." ${ }^{13}$ PISA does not set a proficiency standard. Instead, it sets different levels of performance, ranging from one (the lowest) to six (the highest). A student who is at the proficiency level in math set by NAEP performs moderately above level three on the PISA, which includes students who "can execute clearly described procedures, including those that require sequential decisions. They can select and apply simple problem-solving strategies." ${ }^{14}$ (See sidebar for a detailed statement of the 8th-grade proficiency standard and sample questions from PISA and NAEP that proficient students are expected to pass.)

Given the above definition of math proficiency, U.S. students in the Class of 2011, with a 32 percent proficiency rate, came in 32nd among the nations that participated in PISA. Although performance levels among the countries ranked 23rd to 31 st are not significantly different from that of the United States, 22 countries do significantly outperform the United States in the share of students reaching the proficient level in math. In six countries plus Shanghai and Hong Kong, a majority of students performed at the proficient level, while in the United States less than one-third did. For example, 58 percent of Korean students and 56 percent of Finnish students were proficient. Other countries in which a majority-or near majority-of students performed at or above the proficient

## jurisdictions participating in PISA 2009. (Figure 1)


level included Switzerland, Japan, Canada, and the Netherlands. Many other nations also had math proficiency rates well above that of the United States, including Germany (45 percent), Australia (44 percent), and France (39 percent). Figure 1 presents a detailed listing of the scores of all participating countries as well as the performance of individual states within the United States.

Shanghai topped the list with a 75 percent math proficiency rate, well over twice the 32 percent rate of the United States. However, Shanghai students are from a prosperous metropolitan area within China, with over three times the GDP per capita of the rest of that country, so their performance is more appropriately compared to Massachusetts and Minnesota, which are similarly favored and are the top performers among the U.S. states. When this comparison is made, Shanghai still performs at a distinctly higher level. Only a little more than half (51 percent) of Massachusetts students are proficient in math, while Minnesota, the runner-up state, has a math proficiency rate of just 43 percent. ${ }^{15}$ Only four additional states-Vermont, North Dakota, New Jersey, and Kansas—have a math proficiency rate above 40 percent. Some of the country's largest and richest states score below the average for the United States as a whole, including New York (30 percent), Missouri (30 percent), Michigan (29 percent), Florida (27 percent), and California ( 24 percent). (See Table 1 for a comparison of each state with performances abroad.)
15. Our results are qualitatively similar to those reported by TIMSS 2007, which tested a representative sample of students in Massachusetts and Minnesota. Five countries that had higher average scores than Massachusetts on TIMSS 2007 also took the PISA test. Four of those countries-Taiwan, Korea, Singapore, and Hong Kong-are identified in Figure 1 of this report as outperforming these states on PISA. Japan also outperformed Massachusetts on TIMSS, but we found Japan's performance to be statistically indistinguishable from the Massachusetts' one. Minnesota (whose performance was consistently lower than that of Massachusetts) trailed all five of the above-named countries on both tests, but it outperformed Australia, Sweden and Norway on TIMSS 2007, even though we identified it as not having done that well. In sum, the Massachusetts and Minnesota performances reported here resemble those reported by TIMSS, though Minnesota students seem to have done modestly better on TIMSS than reported here, while the reverse is true for Massachusetts students (Mullis, Martin and Foy, 2008, p. 38).

## Table 1

Percentages of all students in the class of 2011 at the proficient level in math per state. Foreign jurisdictions with similar and higher percentages at the proficient level in math in overall student population.

| Stat |  | Percent proficient | Significantly outperformed by* | Countries with similar percentages of proficient students |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Massachusetts | 50.7 | 6 | Canada - Japan - Netherlands - New Zealand - Switzerland |
| 2 | Minnesota | 43.1 | 11 | Australia - Belgium - France - Germany - Netherlands |
| 3 | Vermont | 41.4 | 14 | Australia - Denmark - Estonia - France - Germany |
| 4 | North Dakota | 41.0 | 16 | Denmark - Estonia - France - Iceland |
| 5 | New Jersey | 40.4 | 14 | Australia - Austria - Denmark - France - Germany |
| 6 | Kansas | 40.2 | 16 | Austria - Denmark - Estonia - France - Slovenia |
| 7 | South Dakota | 39.1 | 16 | Austria - Denmark - France - Hungary - Sweden |
| 8 | Pennsylvania | 38.3 | 16 | Austria - Denmark - France - Hungary - Sweden |
| 9 | New Hampshire | 37.9 | 18 | Austria - Denmark - France - Hungary - Sweden |
| 10 | Montana | 37.6 | 18 | Austria - France - Hungary - Poland - Sweden |
| 11 | Virginia | 37.5 | 17 | Czech Rep - France - Hungary - Poland - Sweden |
| 12 | Colorado | 37.4 | 18 | Austria - France - Hungary - Poland - Sweden |
| 13 | Wisconsin | 37.0 | 18 | Czech Rep - France - Hungary - Poland • Sweden |
| 14 | Maryland | 36.5 | 18 | Czech Rep - France - Hungary - Poland • U.K. |
| 15 | Wyoming | 36.0 | 18 | Czech Rep - France - Poland - Portugal • U.K. |
| 16 | Washington | 35.9 | 19 | Czech Rep - France - Hungary - Poland • U.K. |
| 17 | Ohio | 35.4 | 18 | Czech Rep - France - Poland • Portugal • U.K. |
| 18 | lowa | 35.2 | 19 | Czech Rep - France - Poland - Portugal • U.K. |
| 19 | Indiana | 35.1 | 19 | Czech Rep • France - Poland - Portugal • U.K. |
| 20 | Oregon | 34.8 | 20 | Czech Rep - Hungary - Poland - Portugal • U.K. |
| 21 | Connecticut | 34.7 | 19 | France - Poland - Portugal - Spain - U.K. |
| 22 | Texas | 34.7 | 21 | Czech Rep • Hungary - Poland • Portugal • U.K. |
| 23 | Nebraska | 34.6 | 20 | Czech Rep • Hungary - Poland - Portugal • U.K. |
| 24 | North Carolina | 34.5 | 21 | Czech Rep • Hungary - Poland - Portugal • U.K. |
| 25 | Maine | 34.1 | 22 | Czech Rep • Hungary - Poland - Portugal • U.K. |
| 26 | Idaho | 34.1 | 22 | Czech Rep • Hungary - Poland - Portugal • U.K. |
| 27 | Utah | 32.4 | 26 | Italy • Poland • Portugal - Spain • U.K. |
| 28 | Alaska | 32.2 | 26 | Italy • Poland • Portugal • Spain • U.K. |
|  | United States | 32.2 | 22 | Italy • Latvia • Poland • Spain • U.K. |
| 29 | South Carolina | 31.9 | 26 | Italy • Poland • Portugal - Spain • U.K. |
| 30 | Delaware | 31.3 | 28 | Hungary• Italy - Portugal • Spain • U.K. |
| 31 | Illinois | 30.8 | 27 | Czech Rep - Italy - Portugal • Spain • U.K. |
| 32 | New York | 30.2 | 28 | Hungary•Italy - Portugal • Spain • U.K. |
| 33 | Missouri | 29.9 | 28 | Hungary• Italy• Portugal • Spain • U.K. |
| 34 | Michigan | 28.9 | 30 | Ireland • Italy - Lithuania - Portugal - Spain |
| 35 | Rhode Island | 27.7 | 34 | Latvia - Lithuania |
| 36 | Florida | 27.4 | 34 | Greece - Latvia - Lithuania |
| 37 | Kentucky | 27.3 | 34 | Latvia - Lithuania |
| 38 | Arizona | 26.3 | 34 | Greece - Latvia - Lithuania |
| 39 | Georgia | 24.7 | 35 | Greece - Latvia - Russia |
| 40 | Arkansas | 24.4 | 35 | Croatia - Greece - Israel • Latvia - Russia |
| 41 | California | 23.9 | 36 | Greece - Russia |
| 42 | Tennessee | 23.1 | 36 | Croatia - Greece - Israel • Russia - Turkey |
| 43 | Nevada | 23.0 | 36 | Croatia - Greece - Israel $\bullet$ Russia |
| 44 | Oklahoma | 21.3 | 36 | Croatia - Greece • Israel • Russia - Turkey |
| 45 | Hawaii | 21.2 | 38 | Croatia - Israel • Russia - Turkey |
| 46 | Louisiana | 19.0 | 39 | Bulgaria - Croatia - Israel - Serbia - Turkey |
| 47 | West Virginia | 18.5 | 41 | Bulgaria - Turkey |
| 48 | Alabama | 18.2 | 39 | Bulgaria - Croatia - Israel - Serbia - Turkey |
| 49 | New Mexico | 17.4 | 41 | Bulgaria - Serbia - Turkey |
| 50 | Mississippi | 13.6 | 43 | Bulgaria - Trinidad and Tobago - Uruguay |
| 51 | District of Columbia | 8.0 | 48 | Kazakhstan - Mexico - Thailand |

[^1]Note: List of countries performing at a level that cannot be distinguished statistically are limited to those 5 with the largest population.

## Proficiency in Reading

According to NAEP, students proficient in reading "should be able to make and support inferences about a text, connect parts of a text, and analyze text features." ${ }^{16}$ According to PISA, students at a proficiency level four, a level of performance set very close to NAEP's proficient level, should be "capable of difficult reading tasks, such as locating embedded information, construing meaning from nuances of languages critically evaluating a text." ${ }^{17}$ (See sidebar on page 7 for more specific definitions and sample questions.)

As can be seen in Figure 2, the U.S. proficiency rate in reading, at 31 percent, compares reasonably well to those of most European countries other than Finland. It takes 17 th place among the nations of the world, and only the top 10 countries on PISA outperform the United States by a statistically significant amount. In Korea, 47 percent of the students are proficient in reading. Other countries that outrank the United States include Finland (46 percent), Singapore and New Zealand (42 percent), Japan and Canada (41 percent), Australia (38 percent), and Belgium (37 percent).

Within the United States, Massachusetts is again the leader, with 43 percent of 8th-grade students performing at the NAEP proficient level in reading. Shanghai students perform at a higher level, however, with 55 percent of young people proficient in reading. Within the United States, Vermont is a close second to its neighbor to the south, with 42 percent proficiency. New Jersey and South Dakota come next, with 39 and 37 percent of the students identified as proficient in reading. The District of Columbia, the nation's worst, performs at a level that cannot be distinguished statistically from that of Turkey and Bulgaria. Students living in California (about one-eighth of the U.S. school-age population) are statistically tied with their peers in Slovakia and Spain. See Table 2 for a comparison of how each state fares internationally.

## Performance of U.S. Ethnic and Racial Groups

The percentage proficient in the United States varies considerably across students from different racial and ethnic backgrounds (see Figure 3). While 42 percent of white students were identified as proficient in math, only 11 percent of African American students, 15 percent of Hispanic students, and 16 percent of Native Americans were so identified. Fifty percent of students with an ethnic background from Asia and the Pacific Islands, however, were proficient in math, placing them at a level comparable to all students in Belgium, Canada, and Japan, if lower than that of all students in Korea and Taiwan.

In reading, 40 percent of white students and 41 percent of those from Asia and the Pacific Islands were identified as proficient. Only 13 percent of African


Increasing the percentage of proficient students to the levels attained in Canada and Korea would increase the annual

## U.S. growth rate by

 0.9 percentage points and
## 1.3 percentage points,

 respectively16. NAEP's definitions of the different levels of reading achievement is available at http:// nces.ed.gov/nationsreportcard/reading/ achieveall.asp. Accessed on June 13, 2011. 17. OECD (2000).

## Percentage of students in the class of 2011 at the proficient level in reading in U.S. states and foreign



American students, 5 percent of Hispanic students, and 18 percent of Native American students were so identified.

## White Students

Given the disparate performance among students from various cultural backgrounds, it may be worth inquiring as to whether differences between the United States and other countries are attributable to the substantial minority population within the United States. To examine that question, we compare U.S. white students to all students in other countries. We do this not because we think this is the right comparison, but simply to consider the oft-expressed claim that education problems in the United States are confined to certain segments within the minority community. This is equivalent to the claim that the overall performance of the United States in international comparisons does not take into account the fact that the United States is a much more diverse society than many of the high-performing countries.

While the 42 percent of math proficiency rate for U.S. white students is much higher than the averages for students from African American and Hispanic backgrounds, U.S. white students are still surpassed by all students in 16 other countries. A better than 25-percentage-point gap exists between the performance
jurisdictions participating in PISA 2009. (Figure 2)

of U.S. white students and the percentage of all students deemed proficient in Korea and Finland. White students in the United States trail well behind all students in countries such Japan, Germany, Belgium, and Canada (see Figure A.1).

White students in Massachusetts outperform their peers in other states; 58 percent are at or above the proficient level in math. Maryland, New Jersey, and Texas are the other states in which a majority of white students is proficient in math. Given recent school-related political conflicts in Wisconsin, it is of interest that only 42 percent of that state's white students are proficient in math, a rate no better than the national average.

In reading, the picture looks better. As we mentioned above, only 40 percent of white students are proficient, but that proficiency rate would place the United States at 9th in the world. This proficiency rate does not differ significantly from that for all students in Canada, Japan, and New Zealand, but white students trail in reading, by a significant margin, all students in Korea, Finland, and Singapore. In no state is a majority of white students proficient, although Massachusetts comes close with a 49 percent rate. The four states with the next highest levels of reading proficiency among white students are New Jersey, Connecticut, Maryland, and Colorado. (See Figure A. 2 for the ranking of all the states.)

## NAEP Definition of Reading Proficiency at the 8th Grade Level

Eighth-grade students performing at the proficient level should be able to provide relevant information and summarize main ideas and themes. They should be able to make and support inferences about a text, connect parts of a text, and analyze text features. Students performing at this level should also be able to fully substantiate judgments about content and presentation of content.

## Sample NAEP Question

What is an acceptable way to place a $\$ 1$ Bargain Basement ad in this newspaper?

1. Phone in the ad, pay by credit card
2. Phone in the ad, pay by money order
3. Mail the ad, pay by cash
4. Mail the ad, pay by check

If you chose answer four, you, along
with 31 percent of 8 th graders, got the question correct.

Question from PISA corresponding to the NAEP proficiency level in reading:

## Comparable PISA Question

Question: Underline the sentence that explains what the Australians did to help decide how to deal with the frozen embryos belonging to a couple killed in the plane crash. ${ }^{\text {. }}$ (Answer underlined in red in text to the right.)
i. Cosgrove, Sofroniou, Kelly, and Shiel (2003).

## Technology Creates

 the Need for New RulesScience has a way of getting ahead of law and ethics. That happened dramatically in 1945 on the destructive side of life with the atomic bomb, and is now happening on life's creative side with techniques to overcome human infertility.

Most of us rejoiced with the Brown family in England when Louise, the first testtube baby, was born. And we have marvelled at other firsts-most recently the births of healthy babies that had once been embryos frozen to await the proper moment of implantation in the mother-to-be.

It is about two such frozen embryos in Australia that a storm of legal and ethical questions has arisen. The embryos were destined to be implanted in Elsa Rios, wife of Mario Rios. A previous embryo implant had been unsuccessful, and the Rioses wanted to have another chance at becoming parents. But before they had a second chance to try, the Rioses perished in an airplane crash.

What was the Australian hospital to do with the frozen embryos? Could they be implanted in someone else? There were numerous volunteers. Were the embryos somehow entitled to the Rioses' substantial estate? Or should the embryos be destroyed? The Rioses, understandably, had made no provision for the embryos' future.

The Australians set up a commission to study the matter. Last week, the commission made its report. The embryos should be thawed,

## 'bárgàińásasement

I Use this coupon for items over $\$ 25$ but not more than \$100
13DAYS FOR \$1
| We'll insert your classified ad for 3 consecutive days in the BARGAIN BASEMENT section. To | qualify, the advertised item must be over $\$ 25$ but not more than $\$ 100$ and each item must be priced. | Enclose check or money order with coupon.

1. Print one (1) letter in each space. 4. ALL ADS MUST HAVE PRICE 2. Allow one (1) space between AND PHONE NUMBER IN THEM. 2. Allow one (1) space between 5. No businesses, individuals
words. | 3. Include punctuation marks within the appropriate letter space. only qualify for this rate. 6. Maximum of 3 orders ( 9 insertions) per item.

FIRST LINE

 the panel said, because donation of embryos to someone else would require the consent of

## 3DAYS SPECIAL OFFER FOR FREE

 to respond to the commission recommenda- $\quad$. tion. Should there be an overwhelming outcry against destroying the embryos, the commission would reconsider.Couples now enrolling in Sydney's Queen Victoria hospital for in vitro fertilization programmes must specify what should be done with the embryos if something happens to them.

This assures that a situation similar to the Rioses won't recur. But what of other complex questions? In France, a woman recently had to go to court to be allowed to bear a child from her deceased husband's frozen sperm. How should such a request be handled? What should be done if a surrogate mother breaks her child-bearing contract and refuses to give up the infant she had promised to bear for someone else?

Our society has failed so far to come up with enforceable rules for curbing the destructive potential of atomic power. We are reaping the nightmarish harvest for that failure. The possibilities of misuse of scientists' ability to advance or retard procreation are manifold.

Ethical and legal boundaries need to be set before we stray too far.

## Percentage of students in the class of 2011 in the U.S. at the proficient level in math and reading, by race and ethnicity. (Figure 3)



## Students from College-educated Families

An elite segment of the U.S. population that the NAEP data allow us to isolate consists of students who have at least one parent who has attended college. Given the benefits that accrue to most of those who live in bettereducated families, that segment can be expected to outrank all students in other countries. It may be helpful to think of it as the upper bound of what the U.S. education system has delivered in terms of student performance. Significantly, not even among students from college-educated families can we find a majority of students crossing the proficiency bar in math (see Figure A.3). Only 44 percent of such students did so. In Massachusetts, 61 percent of students from college-educated families are proficient in math. Seven other states have a majority of students from college-educated families performing proficiently in math: Vermont, Minnesota, Kansas, Pennsylvania, Virginia, New Jersey, and Colorado.

In reading, 42 percent of U.S. students from college-educated families in the Class of 2011 are proficient. In two states a majority of these students are proficient in reading: Massachusetts with 57 percent and Vermont with 53 percent. Other high-ranking states include New Jersey, Connecticut, Pennsylvania, Oregon, and Ohio. (See Figure A. 4 for the ranking of all the states.)

## Table 2

Percentages of all students in the class of 2011 at the proficient level in reading per state. Foreign jurisdictions with similar and higher percentages at the proficient level in reading in overall student population.

| State |  | Percent proficient | Significantly outperformed by* | Countries with similar percentages of proficient students |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Massachusetts | 43.0 | 1 | Canada - Finland - Japan - Korea - Singapore |
| 2 | Vermont | 42.1 | 3 | Canada - Japan - Korea - New Zealand - Singapore |
| 3 | New Jersey | 39.0 | 5 | Australia - Belgium - Canada - Japan • Netherlands |
| 4 | Montana | 38.9 | 5 | Australia - Belgium - Canada - Japan - Netherlands |
| 5 | New Hampshire | 37.2 | 8 | Australia - Belgium - Liechtenstein - Netherlands |
| 6 | Connecticut | 37.1 | 7 | Australia - Belgium - France - Japan - Netherlands |
| 7 | Maine | 36.9 | 8 | Australia - Belgium - Liechtenstein - Netherlands |
| 8 | South Dakota | 36.8 | 5 | Australia - Canada - France - Japan • Netherlands |
| 9 | Minnesota | 36.6 | 8 | Australia - Belgium - Liechtenstein - Netherlands |
| 10 | Pennsylvania | 36.4 | 8 | Australia - Belgium - France - Liechtenstein - Netherlands |
| 11 | Ohio | 35.9 | 8 | Australia - Belgium - France - Liechtenstein - Netherlands |
| 12 | lowa | 35.7 | 8 | Australia - Belgium - France - Liechtenstein - Netherlands |
| 13 | Kansas | 35.2 | 9 | Belgium - France - Liechtenstein - Netherlands |
| 14 | Nebraska | 35.0 | 9 | Belgium - France - Liechtenstein - Netherlands |
| 15 | Colorado | 34.6 | 8 | Australia - Belgium - France - Germany - Netherlands |
| 16 | Washington | 34.1 | 10 | France - Germany - Netherlands - Norway - Switzerland |
| 17 | Oregon | 34.0 | 8 | Australia - France - Germany - Poland - Switzerland |
| 18 | Virginia | 33.7 | 9 | Belgium - France - Germany - Netherlands - Poland |
| 19 | Wisconsin | 33.2 | 10 | France - Germany - Hungary - Netherlands - Poland |
| 20 | Wyoming | 33.2 | 10 | France - Germany - Netherlands - Norway - Switzerland |
| 21 | Maryland | 33.2 | 10 | France - Germany - Netherlands - Poland - Sweden |
| 22 | New York | 32.2 | 10 | France - Germany - Hungary - Netherlands - Poland |
| 23 | North Dakota | 32.2 | 10 | France - Germany - Hungary - Netherlands - Poland |
| 24 | Idaho | 31.6 | 10 | France - Germany - Netherlands - Poland - U.K. |
|  | United States | 31.2 | 10 | France - Germany - Netherlands - Poland - U.K. |
| 25 | Indiana | 31.1 | 10 | France - Germany - Netherlands - Poland - U.K. |
| 26 | Missouri | 31.0 | 10 | France - Germany - Netherlands - Poland - U.K. |
| 27 | Delaware | 30.5 | 10 | France - Germany - Netherlands - Poland - U.K. |
| 28 | Utah | 30.1 | 10 | France - Germany - Netherlands - Poland - U.K. |
| 29 | Illinois | 29.8 | 10 | France - Germany - Poland - Taiwan • U.K. |
| 30 | Michigan | 28.2 | 14 | Germany - Italy - Poland - Taiwan • U.K. |
| 31 | Florida | 28.0 | 15 | Italy - Netherlands - Poland - Taiwan - U.K. |
| 32 | North Carolina | 28.0 | 15 | Israel • Italy • Netherlands - Poland - U.K. |
| 33 | Kentucky | 27.7 | 15 | Greece - Italy - Netherlands - Poland - U.K. |
| 34 | Texas | 27.5 | 16 | Greece - Italy - Netherlands - Portugal - U.K. |
| 35 | Rhode Island | 27.2 | 19 | Greece • Hungary • Italy • Portugal • U.K. |
| 36 | Alaska | 27.1 | 19 | Greece • Hungary - Italy - Portugal • U.K. |
| 37 | Oklahoma | 26.1 | 20 | Greece • Hungary - Italy - Portugal - Slovenia |
| 38 | Georgia | 25.6 | 20 | Greece • Hungary - Israel • Italy - Portugal |
| 39 | Tennessee | 25.6 | 20 | Greece - Hungary - Israel • Italy - Portugal |
| 40 | Arkansas | 25.4 | 21 | Greece • Hungary• Israel • Italy - Portugal |
| 41 | South Carolina | 24.6 | 21 | Greece • Hungary - Israel • Italy - Portugal |
| 42 | Arizona | 24.3 | 23 | Denmark - Greece - Israel - Portugal • Spain |
| 43 | West Virginia | 22.9 | 28 | Croatia - Czech Rep - Greece - Portugal - Spain |
| 44 | Nevada | 21.5 | 31 | Austria - Croatia - Czech Rep - Slovakia - Spain |
| 45 | California | 21.5 | 31 | Austria - Croatia - Czech Rep - Slovakia - Spain |
| 46 | Alabama | 21.2 | 31 | Austria - Croatia - Czech Rep - Slovakia - Spain |
| 47 | Hawaii | 20.3 | 34 | Croatia - Latvia - Slovakia |
| 48 | Louisiana | 19.4 | 35 | Croatia - Latvia - Lithuania |
| 49 | Mississippi | 17.4 | 37 | Bulgaria - Croatia - Lithuania - Russia - Turkey |
| 50 | New Mexico | 17.3 | 39 | Bulgaria - Lithuania - Turkey |
| 51 | District of Columbia | 12.1 | 41 | Bulgaria - Chile - Trinidad and Tobago - Turkey |

*Number of countries whose percent proficient was statistically significantly higher
Note: List of countries performing at a level that cannot be distinguished statistically are limited to those 5 with the largest population.

## Are the Proficiency Standards the Same for Math as for Reading?

Has NAEP set a lower proficiency standard in math than in reading? If so, is the math standard too low or the reading bar too high?

At first glance it would seem that the standard is set at pretty much the same level. After all, 32 percent of U.S. students are deemed proficient in math and 31 percent are deemed proficient in reading.

But that coincidence is quite misleading. When compared to peers abroad, the U.S. Class of 2011 performed respectably in reading, trailing only 10 other nations by a statistically significant amount. Admittedly, the United States trails Korea by 16 percentage points, but it's only 9 percentage points behind Canada. Meanwhile, U.S. performance in math is seriously disappointing. It significantly trails that of 22 countries. Korean performance is 26 percentage points higher than that of the United States, while Canadian performance is 17 percentage points higher. Judged by international standards, the U.S. Class of 2011 was clearly doing worse in math than in reading, despite the fact that NAEP reports similar percentages proficient in the two subjects.

A direct comparison of NAEP's proficiency standard with PISA's levels three and four (out of a total of six proficiency levels) also indicates that a lower NAEP bar has been set in math than in reading. To be proficient, one needs to perform at or near the fourth level on PISA's reading exam, but only modestly above the third level on its math exam.

From these findings, we infer that the NAEP experts set an 8th-grade math proficiency standard at a level lower than the one set in reading. Perhaps this is an indication that American society as a whole, including the experts who design NAEP standards, set lower expectations for students in math than in reading. If so, it is a sign that low performance in mathematics within the United States may be deeply rooted in the nation's culture. Those who are setting the common core standards under discussion might well take note of this.

Of course, it could be argued that the math proficiency standard is correct but the reading standard has been set too high. In no country in the world does a majority of the students reach the NAEP proficiency bar set in 8th-grade reading.

## What Do These Findings Mean?

Many have concluded that the productivity of the U.S. economy could be greatly enhanced if a higher percentage of U.S. students were proficient in mathematics. As Michael Brown, Nobel Prize winner in medicine, has declared, "If America is to maintain our high standard of living, we must continue to innovate....


NAEP experts set an 8th-grade math proficiency standard at a level lower than the one set in reading.

"If America is to maintain our high standard of living, we must continue to innovate.... Math and science are the engines of innovation. With these engines we can lead the world."

- Michael Brown, Nobel Prize winner in medicine

18. Quoted at the STEM Education Coalition's website http://www. stemedcoalition.org/, Accessed June 13, 2011.
19. Hanushek. and Woessmann (2008).

Math and science are the engines of innovation. With these engines we can lead the world." ${ }^{18}$

But others have argued that the overall past success of the U.S. economy suggests that high-school math performance is not that critical for sustained growth in economic productivity. After all, U.S. students trailed their peers in the very first international survey undertaken nearly 50 years ago. But that is the wrong message to take away. Other factors contributed to the relatively high rate of growth in economic productivity during the last half of the 20th century, including the openness of the country's markets, respect for property rights, low levels of political corruption, and limited intrusion of government into the operations of the marketplace. The United States, moreover, has always benefited from the in-migration of talent from abroad.

Furthermore, the United States has historically had far higher levels of educational attainment than other countries, with many more students graduating from high school, continuing on to college, and earning an advanced degree. It appears that in the past the country made up for low quality in elementary and high school by educating students for longer periods of time.

As we proceed into the 21 st century, none of these factors remain as favorable to the United States. While other countries are lifting restrictions on market operations, the opposite has been occurring within the United States. The U.S. has also placed sharp limits on the numbers of talented workers that can be legally admitted into the country. Our higher education system, though still perceived to be the best in the world, is recruiting an ever-increasing proportion of its faculty and students from outside the country. Meanwhile, educational attainment rates among U.S. citizens now trail the industrial-world average.

Even if some of these trends can be reversed, that hardly gainsays the desirability of enhancing the mathematical skills of the U.S. student population, especially at a time when the nation's growth in productivity is badly trailing growth rates in China, India, Brazil, and many smaller Asian countries. Eric Hanushek and Ludger Woessmann have shown elsewhere that student performance on international tests such as those we consider here is closely related to long-term economic growth. ${ }^{19}$ Assuming that past trends continue, the country could enjoy a remarkable increment in its annual GDP growth per capita by enhancing the math proficiency of U.S. students. Increasing the percentage of proficient students to the levels attained in Canada and Korea would increase the annual U.S. growth rate by 0.9 percentage points and 1.3 percentage points, respectively (see Figure 4). Since longterm average annual growth rates hover between 2 and 3 percentage points, that increment would lift growth rates by between 30 and 50 percent.

## Estimated increase in U.S. annual economic growth from improved mathematics proficiency. (Figure 4)



Note: Country points indicate the additional \% of students proficient in the United States in order to reach the country's level (X-axis) and corresponding additional growth to be expected on reaching that level ( Y -axis).

When translated into dollar terms, these magnitudes become staggering. If one calculates these percentage increases as national income projections over an 80 -year period (providing for a 20 -year delay before any school reform is completed and the newly proficient students begin their working careers), a back-of-the-envelope calculation suggests gains of nothing less than $\$ 75$ trillion over the period. ${ }^{20}$ That averages out to around a trillion dollars a year. Even if you tweak these numbers a bit in one direction or another to account for various uncertainties, you reach the same bottom line: Those who say that student math performance does not matter are clearly wrong.

Given the integration of the world economy, a global perspective is needed for assessing the performance of U.S. schools, districts, and states. High-school graduates in each and every state compete for jobs with graduates from all over the world. Charles Vest, former president of the at Massachusetts Institute of Technology, has warned, "America faces many challenges...but the enemy I fear most is complacency. We are about to be hit by the full force of global competition. If we continue to ignore the obvious task at hand while others beat us at our own game, our children and grandchildren will pay the price. We must now establish a sense of urgency." ${ }^{21}$
20. For a thorough explanation of this calculation, see Hanushek and Woessmann (2011).
21. Quoted in the STEM Education Coalition's website http://www. stemedcoalition.org/, Accessed June 13, 2011.

## Appendix

## Differences in the Math Performance of the High School Classes of 2009 and 2011

Students are identified as advanced by NAEP only if they score well above the proficient level. Seven percent of U.S. students in the Class of 2011 performed at the advanced level in math (See Figure A.5, Table A.5), a gain of 1 percentage point over the 6 percent identified as advanced in the Class of 2009.

That slight gain is a modest accomplishment, especially given the decline in performance in many other countries. While most changes were small, the percentage of advanced students declined by 2 or more points in the Czech Republic, Austria, Korea, Finland, United Kingdom, Ireland, and Lithuania. Only two of the higher-performing countries, Denmark and Portugal, showed improvement of 2 percentage points or more. Given all these changes, the relative position of the U.S. Class of 2011 improved from the 31st place held by the U. S. Class of 2009 to a tie for 26th place (with Poland, Hungary, Norway, the United Kingdom, Portugal, Italy, and Sweden), despite the inclusion of two new high-scoring PISA participants, Shanghai and Singapore.

Within the United States, little change could be observed between the Class of 2009 and the Class of 2011, apart from the astonishing shift upward in the already high-performing state of Massachusetts, where the percentage advanced rose from 11 percent to 15 percent, a gain unequalled by any other state. Minnesota's performance came in second place in both years, but its students' performance budged northward by only 0.7 percentage points to 11.5 percent for the Class of 2011.

In four other states, scores improved by 2 percentage points or more: Vermont, Maine, North Dakota, and Wyoming (which made a 3.0 gain, the largest gain outside of Massachusetts). It is remarkable how concentrated in certain parts of the country these gains are to be found. If teaching to the talented is a skill, the teachers getting better at the task seem to be concentrated in a few states in New England and the northern plains.

Indeed, the picture that we see of little change in the relative performance of the United States is one that is consistent with the broader trajectory of the United States in international comparisons, which is at best flat and at worst in slight decline over time. Regardless of whether the United States is actually improving in its performance, it is clear that its relative standing with respect to other developed countries is in the bottom half of the OECD countries.

At the same time, we have noted above how a number of other countries, most notably Asian countries such as Taiwan, Singapore, and Japan but also others such Finland and Switzerland or Canada, are significantly ahead of the United States.

## Performing the Crosswalk

Our aim is to compare how students in the different states in the United States are doing with respect to their peers internationally. To obtain this information, we perform a crosswalk between NAEP and the Program for International Student Assessment (PISA), which was administered by the Organization for Economic Co-operation and Development OECD, to representative samples of 15 -year-old students in 65 of the world's school systems, which, to simplify the presentation, we shall refer to as countries. (Hong Kong, Macao, and Shanghai are not independent nations but nonetheless are included in PISA reports.)

The crosswalk is performed by looking at the percentage of U.S. students who reach the proficient level on the NAEP assessment and at the equivalent cutoff score in PISA for that percentage of U.S. students. This gives us the equivalent of the PISA proficiency threshold, allowing us to estimate comparable proficiency rates for all countries and to compare student performance in each of the states within the United States with that of their international peers.

Our analysis relies on test-score information from young adults collected by NAEP and PISA. ${ }^{1}$ NAEP is a large, nationally representative assessment of student performance that has been administered periodically since the early 1970s to U.S. students in 4th grade and 8th grade, and at the age of seventeen. Since 2001, it has provided achievement data for students in each of the 50 states and a select number of urban school districts. PISA is an internationally standardized assessment of student performance in mathematics, science, and reading established by OECD. It was administered in 2000, 2003, 2006 and 2009 to representative samples of 15 -year-olds in all OECD countries as well as in many others. ${ }^{2}$

NAEP is governed by the National Assessment Governing Board (NAGB), which consists of 26 educators and other public figures appointed by the U.S. Secretary of Education. In 2007, NAEP tested representative samples of 8th-grade public and private school students in each of the 50

1. Data for NAEP come from the official website [accessed May 15, 2011], http://nces. ed.gov/nationsreportcard/. NAEP has also tested periodically a representative sample of students in several other subjects.
2. The OECD, which administers PISA, is an international economic organization encompassing most of the high-income, developed countries of the world. In 2009, it had 30 members; three new members (Chile, Israel, and Slovenia) were added in 2010. Sixty-five countries/economies participated in PISA in 2009 (up from 57 in 2006). Data for PISA 2009 come from the PISA microdata (http://www.pisa.oecd.org/). The PISA assessments build upon earlier international testing, most importantly those of the International Association for the Evaluation of Educational Achievement (IEA) now known as Trends in Mathematics and Science Survey (TIMSS). IEA has conducted assessments since the mid-1960s and is responsible for the TIMSS testing that is discussed below. See http://www.iea.nl/. Historical PISA scores and those of TIMSS are summarized in Provasnik, Gonzales, and Miller (2009), which also contains references to the original publications for TIMSS.
3. OECD (2009b). See Chapters 7-9.
4. http://nces.ed.gov/nationsreportcard/, accessed May 18, 2011.
5. National Center for Education Statistics, Report 2008-016, Table C-1.
states, in 10 large public school districts, and in the United States as a whole in math, science, and reading. For each of these jurisdictions, NAEP 2007 calculates the percentage of students who perform at three levels: basic, proficient, and advanced.

Using the NAEP and PISA data for the United States as a whole, the crosswalk exercise identifies an estimated PISA score of 530.7 for math proficiency, as defined by NAEP, and a score of 550.4 for reading proficiency, as defined by NAEP.

With the PISA data, we can obtain an estimate of the percentage of students in those countries above the cutoff, i.e., those who reach the level equivalent to the proficient level in 8th-grade math on NAEP 2007. The shares of students who reach the proficient level in 8 th-grade math in each U.S. state are taken directly from NAEP 2007. It is assumed that both NAEP and PISA tests randomly select questions from a common universe of mathematics knowledge. Given that assumption, it may be further assumed that students who scored similarly on the two exams will have similar math knowledge, i.e., students who scored 530.7 points or better on the PISA test would have been identified as proficient had they taken the NAEP math test. The scaling of PISA straightforwardly reveals that a score of 530.7 points is 31 percent of one standard deviation above the average OECD student score on the PISA, indicating that a somehow accomplished group has been found.

Some of the calculated differences in performance across countries may simply reflect sampling uncertainty or measurement error. We therefore calculate whether the observed differences among states and countries are statistically significant (at the 5 percent level). The requisite standard errors are computed using the methodology described by the OECD. ${ }^{3}$ These standard errors account for both sampling uncertainty (including the two-stage sampling design employed by PISA) and test unreliability (as captured by the five plausible values that represent the underlying probability distribution). NAEP 2007 standard errors are obtained from the NAEP website. ${ }^{4}$

## Identifying the Class of 2011

This crosswalk identifies the relative performance of the Class of 2011. NAEP examinations are given to 8th graders, January through March, when most students are 13 years of age. PISA examinations are given to a random sample of students at the age of 15 , the age at which approximately 70 percent of U . S . students are in 10th grade. ${ }^{5}$ To track the Class of 2011 we rely upon the 2007 NAEP test and the 2009 PISA test. In comparing the performance of the Class
of 2011 on the NAEP and PISA tests at these two different points in time, we assume that no event happened between 8 th and 10th grade that significantly altered the performance of American students relative to that of students in other countries.

Our previous report relied on a similar crosswalk between the PISA 2006 results and the NAEP 2005, a less preferable cohort match but the best possible given the information available in November 2010. ${ }^{6}$ With the appearance of the latest PISA wave in December 2010, we were able to match cohorts more closely, as NAEP data was available for 8 th graders in 2007 while PISA data was available in 2009 for 15-year-olds who are typically in 10th grade. While we are pleased that the cohort match reported in this report is more precise, the findings from this report are consistent with those presented in the previous report. Inasmuch as there are only small differences from one year to the next in the performance of students in particular countries, small variations in the years used to execute a particular cross-walk do not alter findings materially.

## Critiques of PISA

Questions have been raised as to whether any cross-country comparison using PISA data can be meaningful. Prais and others point out that PISA's testing focuses on "real-life" circumstances and on students' capacity to enter the labor market with core skills, such as literacy and numeracy, more than the testing of any specific curriculum. ${ }^{7}$ This inherently favors some countries' specific sequencing of items in the curriculum. For example, Germany's introduction of supplementary questions in the PISA math test (that focused more on arithmetic skills) presents a case of a country that thought that the basic PISA math test was not providing an accurate evaluation of its students' math skills. But too much emphasis on specific questions ignores the commonality of welldesigned tests of student achievement. The TIMSS and PISA tests have quite different designs, but the performance of countries on TIMSS and PISA are highly correlated and both are strongly correlated with a country's economic performance. (See our previous report for further discussion.) ${ }^{8}$ Further, the U.S. National Center for Education Statistics (NCES) is deeply involved in the development of PISA, as it is an active participant in OECD discussions of PISA design; presumably, that office is satisfied that the test is not unfair to U.S. students.

Beyond the appropriateness of the specific PISA questions, worries have been voiced about whether excessive focus on such exams can take away from other educational values that arguably cannot be so readily measured
6. Hanushek, Peterson, and Woessmann (2010).
7. Prais (2003).
8. Hanushek, Peterson, and Woessmann (2010), Appendix.
(i.e., democratic participation, artistic talents, understanding of politics, history, etc). ${ }^{9}$ Goldstein argues that too much importance is attached to PISA: "Perhaps the major [reservation about PISA] centers around the narrowness of its focus, which remains concerned, even fixated, with psychometric properties of a restricted class of conceptually simple models. There is almost no reference [in the official PISA reports] to debates about

Percentage of white students in the class of 2011 in U.S. states at the proficient level in math and


## Percentage of white students in the class of 2011 in U.S. states at the proficient level in reading and


the appropriateness of these models, nor is there reference to methodological and substantive critiques...the usefulness [of such international surveys] must remain in doubt and their value for money somewhat questionable." ${ }^{10}$ Whatever the legitimacy of such concerns, there is little doubt that the acquisition of mathematical and reading skills are fundamental to effective performance in contemporary industrial societies.
10. Goldstein (2004).
percentage of all students at that level in foreign jurisdictions participating in PISA 2009. (Figure A1)

percentage of all students at that level in foreign jurisdictions participating in PISA 2009. (Figure A2)


Percentage of students in the class of 2011 with at least one college-educated parent in U.S. states at the participating in PISA 2009. (Figure A.3)


Percentage of students in the class of 2011 with at least one college-educated parent in U.S. states at participating in PISA 2009. (Figure A.4)


Percentage of students in the class of 2011 at the advanced level in math in U.S. states and foreign


[^2]
## proficient level in math and percentage of all students at that level in foreign jurisdictions


the proficient level in reading and percentage of all students at that level in foreign jurisdictions

jurisdictions participating in PISA 2009. (Figure A.5)


## Table A. 1

Percentages of white students in the class of 2011 at the proficient level in math per state. Foreign jurisdictions with similar and higher percentages at the proficient level in math in overall student population.

| State | Percent proficient | Significantly outperformed by* | Countries with similar percentages of proficient students |
| :---: | :---: | :---: | :---: |
| 1 Massachusetts | 58.0 | 2 | Finland - Korea - Lichtenstein - Netherlands |
| 2 Maryland | 52.9 | 3 | Canada - Japan - Korea - Netherlands - Switzerland |
| 3 Texas | 52.8 | 3 | Canada • Japan • Korea - Netherlands • Switzerland |
| 4 New Jersey | 51.4 | 3 | Belgium - Canada - Japan - Korea - Netherlands |
| 5 Minnesota | 48.2 | 6 | Australia • Canada - Germany • Japan • Netherlands |
| 6 Colorado | 48.0 | 7 | Belgium • Canada • Germany • Japan • Netherlands |
| 7 Virginia | 46.9 | 6 | Australia • Canada - Germany - Japan • Netherlands |
| 8 North Carolina | 46.3 | 7 | Australia - Canada - Germany • Japan • Netherlands |
| 9 Kansas | 46.0 | 9 | Australia • Belgium • Germany • Japan • Netherlands |
| 10 North Dakota | 44.1 | 11 | Australia - Belgium • Germany $\bullet$ Netherlands - New Zealand |
| 11 South Carolina | 43.9 | 11 | Australia - Belgium - France - Germany - Netherlands |
| 12 PennsyIvania | 43.9 | 11 | Australia - Belgium • Germany • Netherlands - New Zealand |
| 13 Connecticut | 43.7 | 11 | Australia - Belgium - France - Germany - Netherlands |
| 14 Alaska | 43.7 | 11 | Australia - Belgium - France - Germany - Netherlands |
| 15 Delaware | 43.2 | 13 | Australia • Estonia • Germany - Netherlands |
| 16 South Dakota | 42.6 | 12 | Australia - Denmark - France - Germany • Netherlands |
| 17 Wisconsin | 42.5 | 13 | Australia - Estonia - France - Germany - Netherlands |
| 18 Vermont | 42.1 | 13 | Australia • Denmark • France - Germany • Netherlands |
| United States | 41.8 | 16 | Estonia |
| 19 Washington | 41.7 | 13 | Australia - Denmark - France - Germany • Netherlands |
| 20 Ohio | 41.6 | 13 | Australia • Austria - France - Germany - Netherlands |
| 21 Montana | 40.9 | 16 | Austria - Denmark - France - Iceland - Slovenia |
| 22 Nebraska | 40.7 | 13 | Australia - Austria - France - Germany - Netherlands |
| 23 Illinois | 40.6 | 12 | Australia - France - Germany • Netherlands - Poland |
| 24 Indiana | 40.4 | 14 | Australia - Austria - Denmark - France - Germany |
| 25 Arizona | 39.5 | 14 | Australia • France - Germany • Hungary - Poland |
| 26 California | 39.5 | 16 | Austria - Denmark - France - Hungary - Sweden |
| 27 New York | 39.1 | 16 | Austria - France - Hungary • Poland • Sweden |
| 28 Oregon | 39.0 | 16 | Austria - Denmark - France - Hungary - Sweden |
| 29 New Hampshire | 38.9 | 16 | Austria • Denmark - France - Slovakia - Slovenia |
| 30 Wyoming | 38.6 | 16 | Austria • France - Hungary - Poland - Sweden |
| 31 lowa | 37.9 | 16 | Czech Rep. • France • Hungary • Poland • Sweden |
| 32 Idaho | 37.8 | 16 | Austria • France - Hungary • Poland • Sweden |
| 33 Florida | 37.5 | 16 | Czech Rep. • France - Poland • Portugal • U.K. |
| 34 Georgia | 37.2 | 16 | Czech Rep. - France - Poland - Portugal • U.K. |
| 35 Missouri | 36.3 | 18 | Czech Rep. - France - Poland - Portugal • U.K. |
| 36 Utah | 36.3 | 18 | Czech Rep. - France - Hungary - Poland • U.K. |
| 37 Michigan | 35.3 | 18 | Czech Rep. - France - Poland - Portugal • U.K. |
| 38 Rhode Island | 34.9 | 20 | Czech Rep. $\bullet$ Hungary • Poland • Portugal • U.K. |
| 39 Maine | 34.7 | 21 | Czech Rep. - Hungary - Poland • Portugal • U.K. |
| 40 New Mexico | 33.2 | 18 | France - Italy • Poland - Spain • U.K. |
| 41 Nevada | 32.1 | 22 | Italy - Poland • Portugal - Spain • U.K. |
| 42 Arkansas | 30.5 | 27 | Czech Rep. - Italy • Portugal • Spain • U.K. |
| 43 Tennessee | 29.7 | 28 | Hungary • Italy • Portugal - Spain • U.K. |
| 44 Kentucky | 29.5 | 30 | Ireland • Italy - Lithuania - Portugal - Spain |
| 45 Louisiana | 28.3 | 28 | Greece - Italy - Portugal - Spain • U.K. |
| 46 Hawaii | 27.6 | 19 | France - Italy - Russia - Turkey - U.K. |
| 47 Alabama | 26.9 | 30 | Greece - Italy - Portugal • Russia - Spain |
| 48 Oklahoma | 25.5 | 34 | Croatia - Greece - Israel • Lithuania - Russia |
| 49 Mississippi | 23.9 | 34 | Croatia - Greece - Israel • Russia - Turkey |
| 50 West Virginia | 19.0 | 41 | Turkey |

[^3]
## Table A. 2

Percentages of white students in the class of 2011 at the proficient level in reading per state. Foreign jurisdictions with similar and higher percentages at the proficient level in reading in overall student population.

| State | Percent <br> proficient | Significantly <br> outperformed by* | Countries with similar percentages <br> of proficient students |
| :--- | :---: | :---: | :---: |
| otp |  |  |  |


| 1 | Massachusetts | 48.8 | 1 | Finland - Korea |
| :---: | :---: | :---: | :---: | :---: |
| 2 | New Jersey | 48.1 | 1 | Finland - Korea |
| 3 | Connecticut | 46.3 | 1 | Finland - Korea |
| 4 | Maryland | 45.4 | 1 | Canada - Finland - Japan - Korea - Singapore |
| 5 | Colorado | 43.4 | 1 | Canada - Finland - Japan - Korea - Netherlands |
| 6 | Texas | 43.3 | 1 | Canada - Finland - Japan - Korea - Netherlands |
| 7 | New York | 42.7 | 1 | Canada - Finland - Japan - Korea - Singapore |
| 8 | Ohio | 41.9 | 1 | Australia - Canada - Japan - Korea - Netherlands |
| 9 | Vermont | 41.8 | 3 | Canada • Japan - Korea - New Zealand - Singapore |
| 10 | Montana | 41.7 | 3 | Canada - Japan - Korea - Netherlands - Singapore |
| 11 | Pennsylvania | 41.3 | 3 | Canada - Japan - Korea - Netherlands - Singapore |
| 12 | Delaware | 41.3 | 3 | Canada - Japan - Korea - Netherlands - Singapore |
| 13 | Minnesota | 40.6 | 4 | Australia - Canada - Japan - Netherlands - Singapore |
| 14 | Virginia | 40.3 | 3 | Australia - Canada - Japan - Korea - Netherlands |
|  | United States | 40.3 | 5 | Canada - Japan • New Zealand |
| 15 | Kansas | 40.2 | 4 | Australia - Canada - Japan - Netherlands - Singapore |
| 16 | Washington | 39.2 | 5 | Australia - Belgium - Canada - Japan • Netherlands |
| 17 | South Dakota | 39.0 | 4 | Australia - Belgium - Canada - Japan - Netherlands |
| 18 | North Carolina | 38.8 | 5 | Australia - Belgium - Canada - Japan - Netherlands |
| 19 | Nebraska | 38.6 | 5 | Australia - Belgium - Canada - Japan • Netherlands |
| 20 | Illinois | 38.2 | 4 | Australia - Belgium - Canada - Japan - Netherlands |
| 21 | lowa | 37.9 | 7 | Australia - Belgium • Japan - Netherlands |
| 22 | Wisconsin | 37.8 | 5 | Australia - Canada - France - Japan • Netherlands |
| 23 | Georgia | 37.8 | 4 | Australia - Canada - France - Japan • Netherlands |
| 24 | Maine | 37.6 | 7 | Australia - Belgium • Japan - Liechtenstein • Netherlands |
| 25 | New Hampshire | 37.4 | 8 | Australia - Belgium • Liechtenstein - Netherlands |
| 26 | Missouri | 37.3 | 8 | Australia - Belgium - Liechtenstein - Netherlands |
| 27 | Arizona | 37.2 | 2 | France - Germany • Japan • Korea - U.K. |
| 28 | Oregon | 37.1 | 5 | Australia • Canada - France - Germany • Japan |
| 29 | Alaska | 36.3 | 8 | Australia - Belgium • France - Liechtenstein - Netherlands |
| 30 | Florida | 36.1 | 8 | Australia - Belgium - France - Germany - Netherlands |
| 31 | Wyoming | 35.8 | 8 | Australia - Belgium - France - Liechtenstein - Netherlands |
| 32 | South Carolina | 35.2 | 8 | Australia - France - Germany • Netherlands - Poland |
| 33 | Indiana | 35.1 | 8 | Australia - Belgium - France - Germany - Netherlands |
| 34 | Rhode Island | 35.0 | 8 | Australia - Belgium - France - Germany - Netherlands |
| 35 | Idaho | 34.4 | 9 | Belgium - France - Germany - Netherlands - Switzerland |
| 36 | Michigan | 33.9 | 9 | Belgium - France - Germany - Netherlands - Poland |
| 37 | California | 33.9 | 10 | France - Germany - Netherlands • Norway - Switzerland |
| 38 | North Dakota | 33.8 | 10 | France - Germany - Netherlands - Poland - Sweden |
| 39 | Utah | 33.2 | 10 | France - Germany - Netherlands - Poland - Sweden |
| 40 | Arkansas | 32.5 | 10 | France - Germany • Netherlands • Poland • Sweden |
| 41 | Tennessee | 32.4 | 10 | France - Germany - Netherlands - Poland - Sweden |
| 42 | Oklahoma | 31.3 | 10 | France - Germany • Netherlands • Poland • U.K. |
| 43 | Hawaii | 30.8 | 8 | France - Germany - Italy - Poland - U.K. |
| 44 | Nevada | 30.0 | 10 | France - Germany - Italy - Poland - U.K. |
| 45 | Kentucky | 29.5 | 10 | France - Germany - Netherlands • Poland • U.K. |
| 46 | New Mexico | 28.9 | 10 | France - Germany - Italy - Poland - U.K. |
| 47 | Mississippi | 28.7 | 10 | France - Germany - Italy - Poland - U.K. |
| 48 | Louisiana | 28.6 | 10 | France - Germany - Italy - Poland - U.K. |
| 49 | Alabama | 28.5 | 11 | Germany - Italy - Netherlands - Poland • U.K. |
| 50 | West Virginia | 23.4 | 26 | Austria - Czech Rep. - Greece - Portugal • Spain |

[^4]
## Table A. 3

Percentages of students in the class of 2011 with at least one college-educated parent at the proficient level in math per state. Foreign jurisdictions with similar and higher percentages at the proficient level in math in overall student population.

| State | Percent proficient | Significantly outperformed by* | Countries with similar percentages of proficient students |
| :---: | :---: | :---: | :---: |
| 1 Massachusetts | 61.1 | 1 | Korea - Liechtenstein - Singapore |
| 2 Vermont | 53.9 | 3 | Finland - Korea - Liechtenstein - Switzerland |
| 3 Minnesota | 53.8 | 5 | Liechtenstein - Switzerland |
| 4 Kansas | 51.3 | 6 | Japan • Liechtenstein - Netherlands - Switzerland |
| 5 New Jersey | 51.1 | 6 | Japan • Liechtenstein - Netherlands - Switzerland |
| 6 Colorado | 50.7 | 6 | Canada • Japan • Liechtenstein • Netherlands - Switzerland |
| 7 Pennsylvania | 50.6 | 6 | Canada • Japan • Liechtenstein • Netherlands - Switzerland |
| 8 Virginia | 50.6 | 6 | Canada - Japan • Liechtenstein • Netherlands - Switzerland |
| 9 Texas | 49.4 | 7 | Canada - Japan - Liechtenstein - Netherlands |
| 10 Indiana | 49.0 | 8 | Belgium - Canada - Japan • Netherlands - New Zealand |
| 11 Maryland | 47.9 | 8 | Belgium - Canada - Japan - Netherlands - New Zealand |
| 12 Wisconsin | 47.7 | 9 | Belgium - Canada - Netherlands - New Zealand |
| 13 New Hampshire | 47.7 | 10 | Belgium - Netherlands - New Zealand |
| 14 Ohio | 47.6 | 10 | Belgium - Netherlands - New Zealand |
| 15 Washington | 47.6 | 9 | Belgium • Canada - Netherlands - New Zealand |
| 16 Montana | 47.4 | 10 | Belgium - Netherlands - New Zealand |
| 17 North Carolina | 47.4 | 8 | Belgium - Canada - Germany • Japan - Netherlands |
| 18 Oregon | 47.4 | 9 | Belgium - Canada - Germany - Netherlands - New Zealand |
| 19 South Dakota | 47.1 | 10 | Belgium - Netherlands - New Zealand |
| 20 North Dakota | 47.1 | 10 | Belgium - Netherlands - New Zealand |
| 21 Connecticut | 47.0 | 10 | Belgium - Netherlands - New Zealand |
| 22 Idaho | 46.7 | 10 | Belgium - Germany - Netherlands - New Zealand |
| 23 Wyoming | 46.1 | 10 | Australia • Belgium - Germany • Netherlands - New Zealand |
| 24 lowa | 45.7 | 12 | Belgium - Germany - New Zealand |
| 25 Illinois | 44.6 | 12 | Australia - Belgium - Germany - New Zealand |
| 26 Nebraska | 44.6 | 14 | Australia - Germany |
| United States | 44.4 | 13 | Australia - Germany • Netherlands |
| 27 Maine | 44.2 | 14 | Australia - Germany |
| 28 South Carolina | 43.0 | 14 | Australia • Estonia - Germany |
| 29 Utah | 43.0 | 14 | Australia - Germany |
| 30 Delaware | 42.7 | 14 | Australia • Estonia - Germany - Iceland |
| 31 Rhode Island | 40.9 | 16 | Estonia - Iceland |
| 32 New York | 40.8 | 16 | Estonia - France - Iceland - Slovenia |
| 33 Missouri | 40.0 | 16 | Denmark • Estonia - France - Iceland - Slovenia |
| 34 California | 39.4 | 18 | Denmark - France - Slovenia |
| 35 Michigan | 38.9 | 17 | Austria - Denmark - France - Iceland - Slovenia |
| 36 Arizona | 38.6 | 18 | Austria - Denmark - France - Slovakia - Slovenia |
| 37 Kentucky | 37.6 | 18 | Austria - Denmark - France - Slovakia - Sweden |
| 38 Florida | 36.5 | 18 | Austria - France - Hungary - Poland - Sweden |
| 39 Nevada | 34.5 | 22 | Czech Rep. - Hungary - Poland - Sweden • U.K. |
| 40 Georgia | 33.9 | 26 | Czech Rep • Hungary • Poland • U.K. |
| 41 Arkansas | 32.5 | 29 | Ireland • Portugal • U.K. |
| 42 Tennessee | 31.9 | 29 | Ireland • Italy - Portugal - Spain • U.K. |
| 43 Oklahoma | 31.6 | 30 | Ireland • Italy • Portugal - Spain |
| 44 New Mexico | 30.2 | 32 | Italy - Spain |
| 45 Hawaii | 28.9 | 34 | Spain |
| 46 West Virginia | 28.8 | 34 | Portugal |
| 47 Alabama | 27.1 | 34 | Latvia - Lithuania |
| 48 Louisiana | 26.3 | 35 | Lithuania |
| 49 Mississippi | 18.8 | 41 | Turkey |
| 50 District of Columbia | 13.2 | 44 | Trinidad and Tobago - Uruguay |

[^5]
## Table A. 4

Percentages of students in the class of 2011 with at least one college-educated parent at the proficient level in reading per state. Foreign jurisdictions with similar and higher percentages at the proficient level in reading in overall student population.

| State | Percent proficient | Significantly outperformed by* | Countries with similar percentages of proficient students |
| :---: | :---: | :---: | :---: |
| 1 Massachusetts | 57.4 | 0 | Shanghai |
| 2 Vermont | 52.7 | 0 | Korea |
| 3 New Jersey | 49.8 | 0 | Finland - Korea |
| 4 Connecticut | 48.6 | 1 | Finland - Korea |
| 5 Pennsylvania | 47.7 | 1 | Finland - Korea |
| 6 Oregon | 47.1 | 1 | Finland - Japan - Korea - New Zealand - Singapore |
| 7 Ohio | 47.1 | 1 | Finland • Japan - Korea - New Zealand - Singapore |
| 8 Montana | 46.9 | 1 | Finland - Korea |
| 9 New Hampshire | 46.8 | 1 | Finland - Korea |
| 10 Maine | 45.8 | 1 | Finland - Japan - Korea - New Zealand - Singapore |
| 11 Kansas | 45.8 | 1 | Finland • Japan • Korea |
| 12 Virginia | 44.3 | 1 | Australia - Canada - Japan - Korea - Netherlands |
| 13 Minnesota | 44.2 | 1 | Finland • Japan - Korea - New Zealand • Singapore |
| 14 Maryland | 44.1 | 1 | Canada - Finland - Japan - Korea - Netherlands |
| 15 Colorado | 44.0 | 1 | Australia - Canada - Japan - Korea - Netherlands |
| 16 lowa | 43.9 | 1 | Canada - Finland - Japan - Korea - Singapore |
| 17 South Dakota | 43.9 | 1 | Australia - Canada - Japan - Korea - Netherlands |
| 18 Washington | 42.9 | 1 | Canada - Finland - Japan - Korea - Netherlands |
| 19 Nebraska | 42.5 | 1 | Canada - Finland • Japan - Korea - Netherlands |
| United States | 42.4 | 4 | Japan • New Zealand • Singapore |
| 20 Texas | 41.7 | 2 | Australia - Canada - Japan - Korea - Netherlands |
| 21 Indiana | 41.4 | 1 | Australia - Canada - Japan - Korea - Netherlands |
| 22 Wisconsin | 41.3 | 1 | Australia - Canada - Japan - Korea - Netherlands |
| 23 New York | 41.3 | 3 | Canada • Japan • Korea - Netherland - Singapore |
| 24 Illinois | 40.5 | 3 | Australia - Canada - Japan - Korea - Netherlands |
| 25 Missouri | 40.0 | 3 | Australia - Canada - Japan - Korea - Netherlands |
| 26 Wyoming | 39.7 | 3 | Australia - Canada - Japan - Korea - Netherlands |
| 27 Idaho | 39.5 | 5 | Australia - Belgium - Canada • Japan • Netherlands |
| 28 Delaware | 39.2 | 3 | Australia - Canada • Japan - Korea - Netherlands |
| 29 Utah | 38.9 | 5 | Australia - Belgium - Canada - Japan • Netherlands |
| 30 Rhode Island | 38.5 | 4 | Australia - Belgium - Canada - Japan • Netherlands |
| 31 North Dakota | 38.4 | 4 | Australia - Canada - France - Japan - Netherlands |
| 32 North Carolina | 37.8 | 5 | Australia - Belgium - Canada - Japan • Netherlands |
| 33 Michigan | 37.6 | 5 | Australia - Canada - France - Japan - Netherlands |
| 34 Arizona | 36.2 | 5 | Canada - France - Germany • Japan • Poland |
| 35 Kentucky | 36.2 | 5 | Australia - Canada - France - Germany - Japan |
| 36 Florida | 35.5 | 8 | Australia - Belgium - France - Germany - Netherlands |
| 37 Oklahoma | 35.4 | 8 | Australia - Belgium - France - Germany - Netherlands |
| 38 California | 34.5 | 8 | Belgium - France - Germany - Netherlands - Switzerland |
| 39 Tennessee | 33.1 | 8 | Australia - France - Germany • Poland • U.K. |
| 40 South Carolina | 32.9 | 8 | Australia - France - Germany • Poland • U.K. |
| 41 Georgia | 32.7 | 9 | France - Germany • Netherlands • Poland • U.K. |
| 42 Arkansas | 31.7 | 10 | France - Germany • Netherlands - Poland • U.K. |
| 43 West Virginia | 31.2 | 10 | France - Germany • Italy • Poland • U.K. |
| 44 Alabama | 28.5 | 10 | France - Germany - Italy - Poland - U.K. |
| 45 Nevada | 28.2 | 10 | France - Germany • Italy - Spain • U.K. |
| 46 Hawaii | 28.0 | 11 | Germany - Italy - Netherlands - Poland - U.K. |
| 47 New Mexico | 26.1 | 15 | Greece - Italy - Netherlands • Poland • U.K. |
| 48 Louisiana | 24.4 | 15 | Italy • Netherlands • Poland • Spain • U.K. |
| 49 Mississippi | 22.5 | 20 | Czech Rep. • Greece • Italy • Portugal • Spain |
| 50 District of Columbia | 18.5 | 34 | Bulgaria - Croatia - Lithuania - Slovakia - Turkey |

[^6]Note: List of countries performing at a level that cannot be distinguished statistically are limited to those 5 with the largest population.

## Table A. 5

Percentages of all students in the class of 2011 at the advanced level in math per state. Foreign jurisdictions with similar and higher percentages at the advanced level in math in overall student population.

| State | Percent advanced | Significantly outperformed by* | Countries with similar percentages of advanced students |
| :---: | :---: | :---: | :---: |
| 1 Massachusetts | 14.9 | 6 | Belgium - Canada - Germany • Japan - Netherlands |
| 2 Minnesota | 11.5 | 14 | Australia - Liechtenstein - Slovenia |
| 3 New Jersey | 10.5 | 15 | France - Iceland • Liechtenstein • Slovakia - Slovenia |
| 4 Vermont | 10.3 | 15 | Austria • France - Iceland • Slovakia - Slovenia |
| 5 Maryland | 10.1 | 15 | Austria - Czech Rep - France - Slovakia - Slovenia |
| 6 Colorado | 9.5 | 16 | Austria - Czech Rep - France - Iceland • Slovakia |
| 7 Washington | 9.1 | 17 | Austria - Czech Rep - Denmark - France - Sweden |
| 8 Virginia | 8.9 | 17 | Austria - Czech Rep - Denmark - France - Sweden |
| 9 Kansas | 8.5 | 17 | Austria - Czech Rep - Denmark - France - Sweden |
| 10 Oregon | 8.5 | 17 | Austria • Czech Rep - Denmark - France - Sweden |
| 11 Connecticut | 8.4 | 18 | Czech Rep - Denmark - France - Hungary • Sweden |
| 12 North Carolina | 8.0 | 19 | Czech Rep • Denmark • Hungary • Poland • Sweden |
| 13 Wisconsin | 8.0 | 20 | Czech Rep • Denmark - Hungary • Poland • Sweden |
| 14 Pennsylvania | 7.9 | 20 | Czech Rep • Denmark - Hungary • Poland • Sweden |
| 15 New Hampshire | 7.8 | 20 | Czech Rep • Denmark • Hungary • Poland • Sweden |
| 16 Nebraska | 7.6 | 21 | Denmark • Hungary - Norway • Poland • Sweden |
| 17 Indiana | 7.5 | 21 | Hungary • Poland • Portugal • Sweden • U.K. |
| 18 South Carolina | 7.4 | 21 | Hungary • Poland • Portugal • Sweden • U.K. |
| 19 Montana | 7.2 | 26 | Hungary - Norway • Poland • Portugal • U.K. |
| 20 Maine | 7.1 | 25 | Hungary • Poland • Portugal • Sweden • U.K. |
| 21 Alaska | 7.1 | 26 | Hungary • Norway • Poland • Portugal • U.K. |
| 22 lowa | 7.1 | 26 | Hungary $\bullet$ Norway • Poland • U.K. |
| United States | 7.0 | 25 | Hungary • Italy • Poland • Portugal • U.K. |
| 23 Illinois | 7.0 | 25 | Hungary • Poland • Portugal • Sweden • U.K. |
| 24 Texas | 6.9 | 26 |  |
| 25 South Dakota | 6.9 | 26 | Hungary • Norway • Poland • Portugal • U.K. |
| 26 North Dakota | 6.8 | 26 | Hungary • Italy • Poland • Portugal • U.K. |
| 27 Delaware | 6.6 | 26 | Italy • Poland • Portugal - Turkey • U.K. |
| 28 New York | 6.6 | 26 | Hungary • Italy • Poland • Portugal • U.K. |
| 29 Wyoming | 6.5 | 26 | Hungary • Italy • Poland • Portugal • U.K. |
| 30 Ohio | 6.5 | 26 | Hungary • Italy • Poland • Portugal • U.K. |
| 31 Idaho | 6.2 | 28 | Hungary • Italy • Portugal • U.K. |
| 32 Utah | 6.1 | 28 | Hungary • Italy • Portugal • U.K. |
| 33 Michigan | 6.0 | 28 | Hungary • Italy • Portugal • U.K. |
| 34 Florida | 5.4 | 32 | Lithuania - Spain - Turkey |
| 35 Missouri | 5.3 | 32 | Lithuania - Spain - Turkey |
| 36 Kentucky | 5.0 | 32 | Lithuania - Spain - Turkey |
| 37 Rhode Island | 4.9 | 32 | Lithuania - Spain - Turkey |
| 38 California | 4.9 | 33 | Lithuania - Turkey |
| 39 Arizona | 4.8 | 32 | Ireland - Lithuania - Spain - Turkey |
| 40 Georgia | 4.1 | 33 | Greece • Ireland • Israel • Russia - Turkey |
| 41 Tennessee | 3.8 | 35 | Greece • Ireland • Israel • Russia - Turkey |
| 42 Arkansas | 3.7 | 35 | Greece • Ireland • Israel • Russia - Turkey |
| 43 Nevada | 3.6 | 35 | Greece • Ireland • Israel • Russia - Turkey |
| 44 Oklahoma | 3.1 | 39 | Bulgaria - Croatia • Russia - Turkey |
| 45 Hawaii | 3.0 | 40 | Bulgaria - Croatia - Turkey |
| 46 New Mexico | 2.6 | 42 | Bulgaria - Serbia |
| 47 Alabama | 2.5 | 42 | Bulgaria - Serbia |
| 48 Louisiana | 2.2 | 42 | Bulgaria - Serbia |
| 49 West Virginia | 2.2 | 42 | Bulgaria - Serbia |
| 50 Mississippi | 1.6 | 44 | Trinidad and Tobago - Uruguay |
| 51 District of Columbia | 1.1 | 47 | Dubai |

*Number of countries whose percent advanced was statistically significantly higher
Note: List of countries performing at a level that cannot be distinguished statistically are limited to those 5 with the largest population.

## References

Bartsch, Kristina (2009): "Employment projections, 2008-18," Monthly Labor Review November.

Cosgrove, Judith, Nick Sofroniou, Amy Kelly, and Gerry Shiel (2003): A teacher's guide to the reading literacy achievements of Irish 15-year-olds. Educational Research Center: Dublin.

Goldstein, Harvey (2004): "International comparisons of student attainment: some issues arising from the PISA study," Assessment in Education 11.3.

McKinsey Global Institute (2011): "Growth and renewal in the United States: Retooling America's economic engine," February 2011. (available at http://www. mckinsey.com/mgi)

Hanushek, Eric, Paul Peterson, and Ludger Woessmann (2010): U. S. Math Performance in global perspective: How well does each state do at producing high-achieving students? Harvard's Program on Education Policy and Governance Report No.: 10-19.

Hanushek, Eric and Ludger Woessmann (2008): "The role of cognitive skills in economic development". Journal of Economic Literature, 46:3.

Hanushek, Eric A. and Ludger Woessmann (2011): "How much do educational outcomes matter in OECD countries?" Economic Policy, no. 67 (July), 1-65.

Lingiard, Bon and Grek, Sotiria (2007): "The OECD, indicators and PISA: An exploration of events and theoretical perspectives" ESRC/ESF Research Project on Fabricating Quality in Education Working paper 2, http://www.ces.ed.ac.uk/ PDF\%20Files/FabQ_WP2.pdf

Mullis, Ina, V. S., Michael O. Martin and Pierre Foy, (2008): TIMMS 2007 International Mathematics Report: Findings from IEA's Trends in International Mathematics and Science Study at the Fourth and Eighth Grades. International Association for the Evaluation of Educational Achievement.

Shiel, G., R. Perkins, S. Close, , and E. Oldham (2007): "PISA Mathematics: A Teacher's Guide" Ireland's Department of Education and Science.

OECD (2009a): PISA 2009 assessment framework: Key competencies in reading, mathematics and science. Paris: OECD.

OECD (2009b): PISA Data Analysis Manual. Paris: OECD.
OECD (2000): Knowledge and skills for life: First results from PISA 2000. Paris: OECD.
Prais, Sig (2003): "Cautions on OECD'S recent educational survey (PISA)". Oxford Review of Education, Vol. 29, No. 2.

Provasnik, Stephan, Patrick Gonzales, and David Miller (2009): U. S. performance across international assessments of student achievement: Special supplement to the Condition of Education 2009. Washington, DC: National Center for Education Statistics.

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[^1]:    *Number of countries whose percent proficient was statistically significantly higher

[^2]:    Note: Excludes participating countries below 1 percent.

[^3]:    *Number of countries whose percent proficient was statistically significantly higher
    Note: List of countries performing at a level that cannot be distinguished statistically are limited to those 5 with the largest population.

[^4]:    *Number of countries whose percent proficient was statistically significantly higher
    Note: List of countries performing at a level that cannot be distinguished statistically are limited to those 5 with the largest population.

[^5]:    *Number of countries whose percent proficient was statistically significantly higher
    Note: List of countries performing at a level that cannot be distinguished statistically are limited to those 5 with the largest population.

[^6]:    *Number of countries whose percent proficient was statistically significantly higher

